

$$\begin{vmatrix} 0 & x & y & z \\ x & 0 & z & y \\ y & z & 0 & x \\ z & y & x & 0 \end{vmatrix} = \begin{vmatrix} 0 & x & y & z \\ 1 & 0 & \frac{z}{x} & \frac{y}{x} \\ 1 & \frac{z}{x} & 0 & \frac{x}{y} \\ 1 & \frac{y}{x} & \frac{x}{y} & 0 \end{vmatrix} \cdot xyz = \begin{vmatrix} 0 & xyz & xyz & xyz \\ 1 & 0 & z^2 & y^2 \\ 1 & 2^2 & 0 & x^2 \\ 1 & y^2 & x^2 & 0 \end{vmatrix} \cdot \frac{xyz}{2x \cdot 2y \cdot xy}$$

$\downarrow$

$\cdot 2y \cdot 2x \cdot xy$

$x, y, z \neq 0$

$$\begin{vmatrix} 0 & xyz & xyz & xyz \\ 1 & 0 & z^2 & y^2 \\ 1 & z^2 & 0 & x^2 \\ 1 & y^2 & x^2 & 0 \end{vmatrix} \cdot \frac{1}{xyz} = \begin{vmatrix} 0 & 1 & 1 & 1 \\ 1 & 0 & z^2 & y^2 \\ 1 & z^2 & 0 & x^2 \\ 1 & y^2 & x^2 & 0 \end{vmatrix}$$

Obecno:

$$p(x, y, z) \rightarrow p(x, y, z) \frac{xyz}{xyz} \rightarrow p(x, y, z)$$

toto není definované!!

②

$$A = \begin{pmatrix} 1 & 0 & 1 \\ -2 & 1 & 0 \\ 0 & 1 & 1 \end{pmatrix} \quad \text{adj}(A) = \begin{pmatrix} 1 & +1 & -1 \\ +2 & 1 & -2 \\ -2 & -1 & 1 \end{pmatrix}$$

$$\frac{\text{adj}(A)}{Z_5} = \begin{pmatrix} 1 & 1 & 1 \\ 2 & 1 & 3 \\ 3 & 1 & 1 \end{pmatrix}$$

$$|A| = -1 \quad A^{-1} = \begin{pmatrix} -1 & -1 & 1 \\ -2 & -1 & 2 \\ 2 & 1 & -2 \end{pmatrix}$$

$$|A| = 5 \quad A^{-1} = \begin{pmatrix} 1 & 1 & 1 \\ 3 & 5 & 2 \\ 2 & 1 & 5 \end{pmatrix}$$

$$\begin{pmatrix} 1 & 0 & 2 \\ 1 & 2 & 0 \\ 0 & 1 & 1 \end{pmatrix} \quad \text{adj}(A) = \begin{pmatrix} 2 & 2 & -5 \\ -1 & 1 & 2 \\ 1 & -1 & 2 \end{pmatrix} \quad \text{adj}(A) = \begin{pmatrix} 2 & 2 & 1 \\ 5 & 1 & 2 \\ 1 & 5 & 2 \end{pmatrix}$$

$$\textcircled{3} \quad a(3,1,1)^T, b(2,1,1)^T, c(2,3,2)^T$$

$$\begin{vmatrix} 3 & 2 & 2 \\ 1 & 1 & 3 \\ 1 & 1 & 2 \end{vmatrix} = 1 \quad \rightarrow \text{tzn. } \text{že tento rozměrnostní matici objeví 1.}$$

$$\textcircled{4} \quad f: \mathbb{R}^3 \rightarrow \mathbb{R}^3$$

Determinant reprezentuje minimální/vzdálenostní objemu.

$$(1,3,1)^T \quad (3,1,0)^T$$

$$(1,0,3)^T \rightarrow (1,0,2)^T$$

$$(1,1,1)^T \quad (5,1,5)^T$$

$$V(A) = \frac{5}{3}\pi, \quad V(f(A)) = |\det(f(A))| \cdot V(A) = \pi$$

$$[f] \cdot A = B$$

$$[f] = B \cdot A^{-1} = \frac{\det(B)}{\det(A)}$$


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$$\begin{matrix} 1 & 1 & 1 \\ 3 & 0 & 1 \\ 1 & 3 & 1 \end{matrix} = \begin{matrix} 1 & 1 & 1 \\ 0 & -3 & -2 \\ 0 & 2 & 0 \end{matrix} = \begin{matrix} 1 & 1 & 1 \\ 0 & -1 & -2 \\ 0 & 2 & 0 \end{matrix}$$

$$= \begin{matrix} 1 & 1 & 1 \\ 0 & 0 & -2 \\ 0 & 2 & 0 \end{matrix} = \begin{matrix} 1 & 1 & 1 \\ 0 & 2 & 0 \\ 0 & 0 & -2 \end{matrix} = \underline{\underline{5}}$$

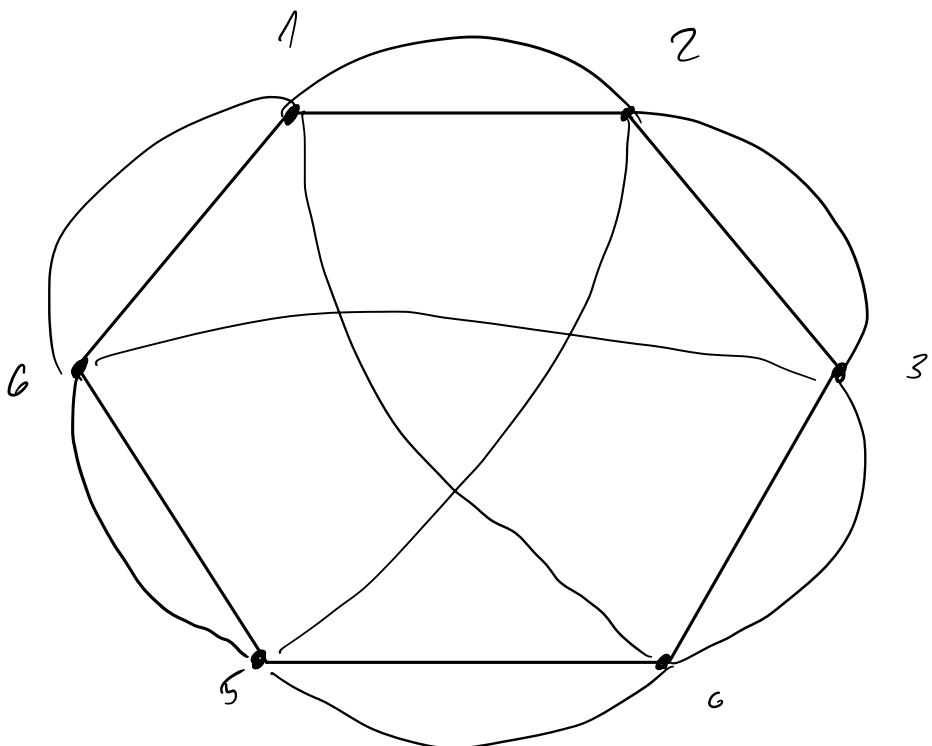
$\curvearrowright$

$$\det(A \cdot B) = \det(A) \cdot \det(B)$$

$$\det(A^{-1}) = \frac{1}{\det(A)}$$

$\curvearrowright$

$$\begin{matrix} 3 & 1 & 5 \\ 1 & 0 & 1 \\ 0 & 2 & 5 \end{matrix} = \underline{\underline{-3}}$$



$$H(6) = \det(L_6^{1,1}) = 960$$

$$\left( \begin{array}{cccccc} 1 & -2 & 0 & -1 & 0 & -2 \\ -2 & 5 & -2 & 0 & -1 & 0 \\ 0 & -2 & 5 & -2 & 0 & -1 \\ -1 & 0 & -2 & 5 & -2 & 0 \\ -2 & 0 & -1 & 0 & -5 & 5 \end{array} \right)$$

⑦  $\mathbb{Z}_5$   
 $p(x) = 4x^{20} + 3x^{17} + 2x^{16} + x^{13} + 3x^{12} + 2x^{10} + 4x^9 + 2x^7 + 2x^5 + x + 3.$

$a \in \mathbb{Z}_p : a^{p-1} = 1$   
 $a \neq 0$   
 $a^p = a$   
 $x^p = x$

$$p^1(x) = a_4 \cdot x^4 + a_3 \cdot x^3 + a_2 \cdot x^2 + a_1 \cdot x^1 + a_0$$

$$a_0 = 3$$

$$p^1(x) = 4x^4 + 2x^3 + 2x^2 + x + 3$$

$$a_1 = 3 + 1 + 4 + 2 + 1 = 1$$

$$a_2 = 2$$

$$a_3 = 2$$

$$a_4 = 4 + 2 + 3 = 4$$

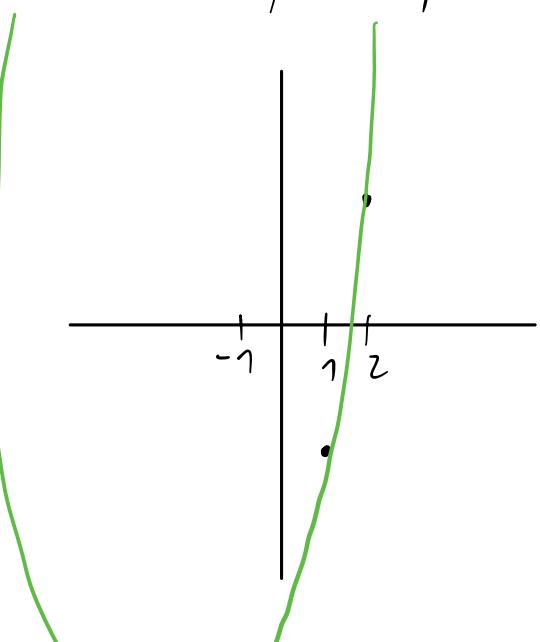
$$a^{p-1} = 1$$

jsem v  $\mathbb{Z}_5$ , false

$$x^{20} = x^{16} = x^{12} = x^8 = x^4 = x$$

Reducujeme stupně!

⑨ a)  $(x_1, y_1), (x_2, y_2), (x_3, y_3)$



$$p(x) = ?$$

$$\rho_1 = \frac{(x-x_2)(x-x_3)}{(x_1-x_2) \cdot (x_1-x_3)} = \frac{x^2 - 3x + 2}{6}$$

$$\rho_2 = \frac{(x-x_1) - (x-x_3)}{(x_2-x_1) \cdot (x_2-x_3)} = -x^2 + x + 2$$

$$\rho_3 = \frac{(x-x_1) \cdot (x-x_2)}{(x_3-x_1) \cdot (x_3-x_2)} = \frac{x^2 - 1}{3}$$

$$p = -9 \cdot \rho_1(x) - 3 \cdot \rho_2(x) + 3 \cdot \rho_3(x) = 2x^2 - 3x + 5$$